

# Two-Player Perfect Information Games: A Brief Survey

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# Abstract

- Domain: two-player games.
- Which game characters are predominant when the solution of a game is the main target?
  - It is concluded that **decision complexity** is more important than **state-space complexity**.
  - There is a trade-off between **knowledge-based methods** and **brute-force methods**.
  - There is a clear correlation between the first-player's **initiative** and the necessary effort to solve a game.

# Domain of studies

- Domain: 2-person **zero-sum** games with **perfect information**.
  - Result: win, loss or draw.
  - **Zero-sum** means one player's loss is exactly the other player's gain, and vice versa.
    - ▷ *There is no way for both players to win at the same time.*
    - ▷ *In this case, it is usually called a tie or draw.*

# Complexity of a game

- **State-space** complexity of a game: the number of the **legal positions** in a game.
  - A **legal position** is one that can be reached from the initial position.
  - Often it is difficult to decide whether one can be reached from the initial position or not, instead we use all possible arrangements.
- **Game-tree** (or **decision**) complexity of a game: the number of the nodes in a **solution search tree**.
  - Actually, it is usually a game **graph**, not tree.
  - A solution search tree is a tree where the game-theoretic value of the root position can be decided.
  - Each node in the tree is a legal position. The children of a parent node  $P$  are the positions that  $P$  can reach in one step.
    - ▷ *Some children of a node may not be in a solution search tree.*
    - ▷ *For example, if facing a position, one can capture the opponent's king and thus wins in Chess, but he makes other move and as a result his king is captured in the next ply.*
  - Some legal states may not be in a solution search tree.
    - ▷ *These are **unreasonable** positions.*

# Game-theoretic value

- **Game-theoretic value** of a game: the outcome, i.e., win, loss or draw, when all participants play optimally.
  - Classification of games' solutions according to L.V. Allis [Ph.D. thesis 1994] if they are considered solved.
    - ▷ *Ultra-weakly solved*: the game-theoretic value of the initial position has been determined.
    - ▷ *Weakly solved*: for the initial position a strategy has been determined to achieve the game-theoretic value against any opponent.
      - ▷ *The strategy must be efficient and practical in terms of resource usage.*
    - ▷ *Strongly solved*: a strategy has been determined for all legal positions.
  - The game-theoretical values of most games are **unknown** or are only known for some **legal positions**.

# Definitions

- **Initiative:** the right to move first.
  - Many games are known to be favor to the player who plays first.
    - ▷ *Go-Moku.*
  - Only very few games are known to be favor to the second player.
    - ▷ *6 by 6 Othello.*
- A **fair** game: the game-theoretic value is draw and both players have roughly an equal probability to make a mistake.
  - People normally enjoy playing fair games over unfair ones.
  - Examples:
    - ▷ *Paper-scissor-stone.*
    - ▷ *Roll a dice and the one getting a larger number wins.*
    - ▷ *Nine Men's Morris (proven in 1995)*
    - ▷ *Checkers (proven in 2007)*
  - Many popular games are not fair or are unknown of their fairness.
  - It is difficult to prove a non-trivial game is fair or to design a non-trivial fair one.
- An **asymmetric** game
  - An asymmetric game is one that has different rules for the two players.
  - Examples: Renju, Go with a non-zero Komi value.

# More definitions (1/2)

- A **convergent** game: the size of the state space decreases as the game progresses.
  - Start with many pieces on the board and pieces are gradually removed during the course of the game.
    - ▷ *Example: Checkers.*
  - It means the number of possible configurations decreases as the game progresses.
- A **divergent** game: the size of the state space increases as the game progresses.
  - May start with an empty board, and pieces are gradually added during the course of the game.
    - ▷ *Example: Connect-5 before the board is almost filled.*
  - It means the number of possible configurations increases as the game progresses.
    - ▷ *For Chinese chess, a rook can visit more places when it is away from its initial location.*

# More definitions (2/2)

- A game may be convergent at one stage and then divergent at other stage.
  - Most games are dynamic.
  - For the game of Tic-Tac-Toe, assume you have played  $x$  plys with  $x$  being even.
    - ▷ *Then you have a possible of*

$$\begin{pmatrix} 9 \\ x/2 \end{pmatrix} \begin{pmatrix} 9 - x/2 \\ x/2 \end{pmatrix}$$

different configurations.

- This number is not monotone increasing or decreasing.



# Predictions made in 1990

- Predictions were made in 1990 [Allis et al 1991] for the year 2000 concerning the expected playing strength of computer programs.

solved	over champion	world champion	grand master	amateur
Connect-four	Checkers (8 * 8)	Chess	Go (9 * 9)	Go (19 * 19)
Qubic	Renju	Draughts (10 * 10)	Chinese chess	
Nine Men's Morris	Othello		Bridge	
Go-Moku	Scrabble			
Awari	Backgammon			

- ▷ *Over champion means definitely over the best human player.*
- ▷ *World champion means equaling to the best human player.*
- ▷ *Grand master means beating most human players.*

# A double dichotomy of the game space

$\log \log(\text{state-space complexity}) \uparrow$

<b>category 3</b> if solvable at all, then by knowledge-based methods	<b>category 4</b> currently unsolvable by any method
<b>category 1</b> solvable by any method	<b>category 2</b> if solvable at all, then by brute-force methods

$\log \log(\text{game-tree complexity}) \rightarrow$

# Questions to be researched

- Can perfect knowledge obtained from solved games be translated into rules and strategies which human beings can assimilate?
- Are such rules generic, or do they constitute a multitude of ad hoc recipes?
- Can methods be transferred between games?
  - More specifically, are there generic methods for all category- $i$  games, or is each game in a specific category a law unto itself?

# Convergent games

- Since most games are dynamic, here we consider games whose ending phases are convergent.
  - Can be solved by the method of **endgame databases** if we can enumerate and store all possible positions at a certain stage.
- Problems solved:
  - Nine Men's Morris: in the year 1995, a total of 7,673,759,269 states.
    - ▷ *The game theoretic value is draw.*
  - Mancala games
    - ▷ *Awari: in the year 2002.*
    - ▷ *Kalah: in the year 2000 upto, but not equal, Kalah(6,6).*
  - Checkers
    - ▷ *By combining endgame databases, middle-game databases and verification of opening-game analysis.*
    - ▷ *Solved the so called 100-year position in 1994.*
    - ▷ *The game is proved to be a draw in 2007.*
  - Chess endgames
  - Chinese chess endgames

# Divergent games

- Since most games are dynamic, here we consider games whose INITIAL phases are divergent.
- Connection games
  - Connect-four ( $6 * 7$ )
  - Qubic ( $4 * 4 * 4$ )
  - Go-Moku ( $15 * 15$ )
  - Renju
  - $k$ -in-a-row games
  - Hex ( $10 * 10$  or  $11 * 11$ )
- Polynmino games: place pieces inside a board without overlapping and alternatively until one cannot place more.
  - Pentominoes
  - Domineering
- Othello
- Chess
- Chinese chess
- Shogi
- Go

# Connection games (1/2)

## ■ Connect-four ( $6 * 7$ )

- Solved by J. Allen in 1989 using a brute-force depth first search with alpha-beta pruning, a transposition table, and killer-move heuristics.
- Also solved by L.V. Allis in 1988 using a knowledge-based approach by combining 9 strategic rules that identify potential **threats** of the opponent.
  - ▷ *Threats are something like forced moves or moves you have little choices.*
  - ▷ *Threats are moves with predictable counter-moves.*
- It is first-player win.
- Weakly solved on a SUN-4 workstation using 300+ hours.

## ■ Qubic ( $4 * 4 * 4$ )

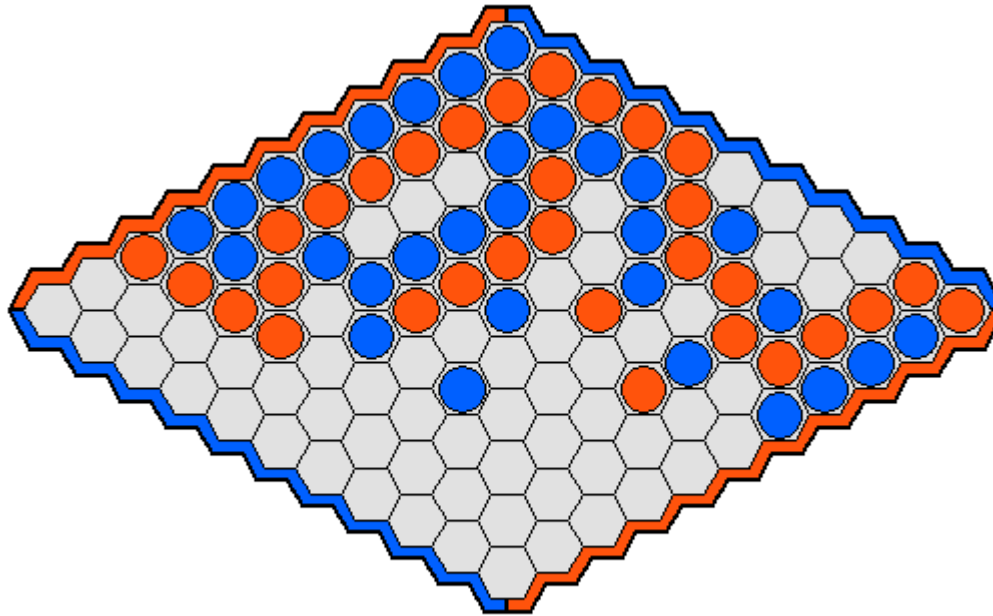
- A three-dimensional version of Tic-Tac-Toe.
- Connect-four played on a  $4 * 4 * 4$  game board.
- Solved in 1980 by O. Patashnik by combining the usual depth-first search with expert knowledge for ordering the moves.
  - ▷ *It is first-player win for the 2-player version.*

# Connection games (2/2)

- **Go-Moku (15 \* 15)**
  - First-player win.
  - Weakly solved by L.V. Allis in 1995 using a combination of threat-space search and database construction.
- **Renju**
  - Does not allow the first player to play certain moves.
  - An **asymmetric** game.
  - Weakly solved by Wágner and Virág in 2000 by combining search and knowledge.
    - ▷ *Took advantage of an iterative-deepening search based on threat sequences up to 17 plies.*
    - ▷ *It is still first-player win.*
- **$k$ -in-a-row games**
  - $mnk$ -Game: a game playing on a board of  $m$  rows and  $n$  columns with the goal of obtaining a straight line of length  $k$ .
  - Variations: first ply picks only one stone, the rest of the plies pick two stones at one time.
    - ▷ *Connect 6.*
    - ▷ *Try to balance the advantage of the initiative!*

# Hex (10 \* 10 or 11 \* 11)

- Invented in 1942 by Peit Hein and John Hash (source: wiki)
- Rules
  - Two players place one piece of each one's color alternatively.
  - A player connects the NW and SE sides, while the other one connects the NE and SW sides. One who can do so wins.



Red won

Courtesy of ICGA web site



# HEX: properties

## ■ Revised rules:

- ▷ *When the first player wins, allow the second player to play one more time. If the second player also wins, then the game is tie.*
- ▷ *When the board is full and no one wins, then it is also a tie.*

## ■ Properties:

- It is a finite game.
- It is not possible for both players to win at the same time.
- Exactly one of the players can win.

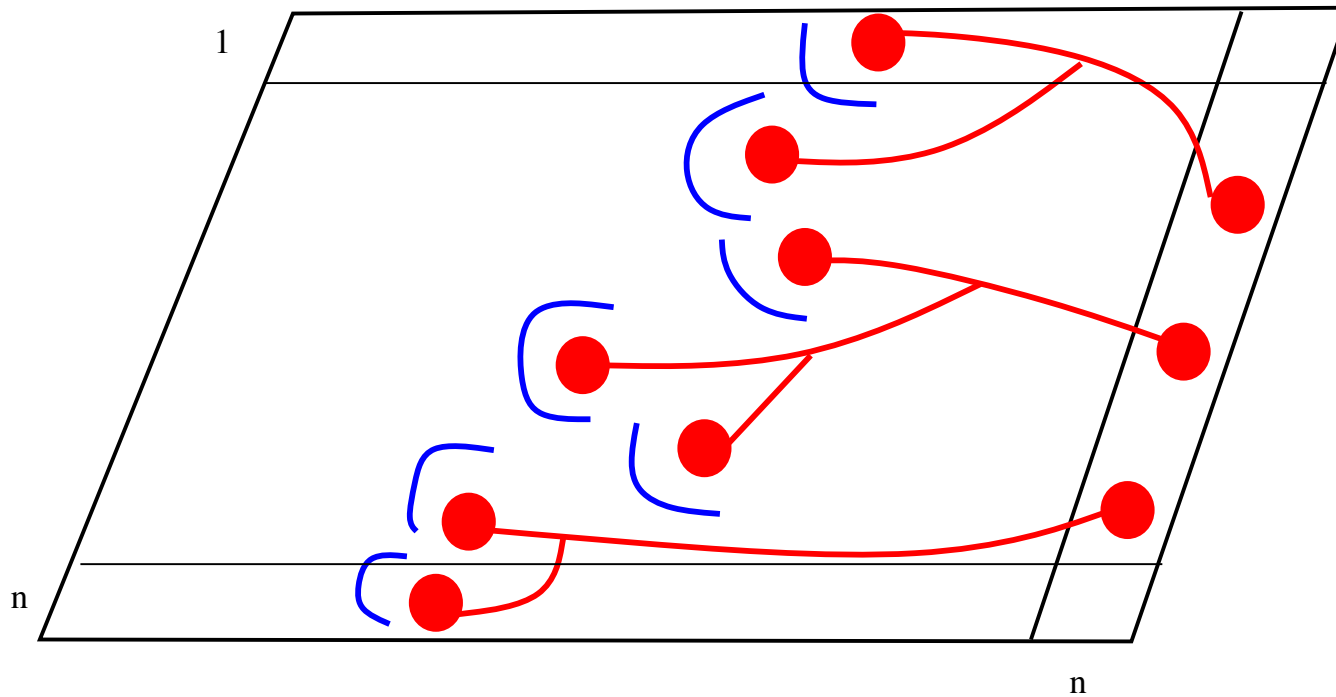
# Proof on exactly one player win (1/2)

- It is easy to know there cannot be two winners.
- A topological argument.
  - A vertical chain can only be cut by a horizontal chain and vice versa because each cell is connected with 6 adjacent cells.
    - ▷ *Note if a cell has 4 neighbors as in the case of Go, then it is possible to cut off a vertical chain by cells that are not horizontally connected and vice versa.*
- Other arguments such as one using graph theory exist.

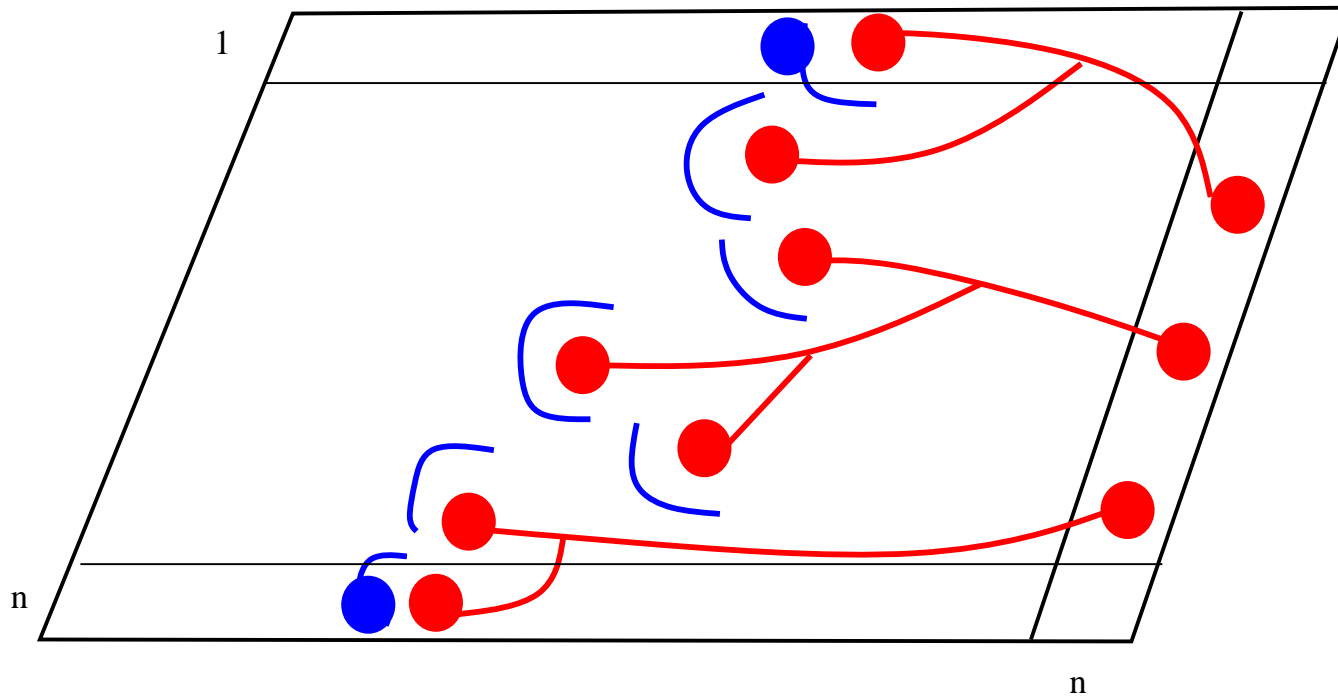
# Proof on exactly one player win (2/2)

- We then prove there is at least one winner.
  - Assume there is no winner when the board is full.
- W.l.o.g. let  $R$  be the set of red cells that can be reached by chains originated from the rightmost column.
  - $R$  must contain a cell of the rightmost column; otherwise we have a contradiction which means the blue wins.
- Let  $N(R)$  be the blue cells that can be reached by  $R$  originated from the rightmost column.
  - $N(R)$  must contain a cell in the top row.
    - ▷ Otherwise,  $R$  contains all cells in the first row, which is a contradiction.
  - $N(R)$  must contain a cell in the bottom row.
    - ▷ Otherwise,  $R$  contains all cells in the bottom row, which is a contradiction.
  - $N(R)$  must be connected.
    - ▷ Otherwise,  $R$  can advance further.
  - Hence  $N(R)$  is a blue winning chain.

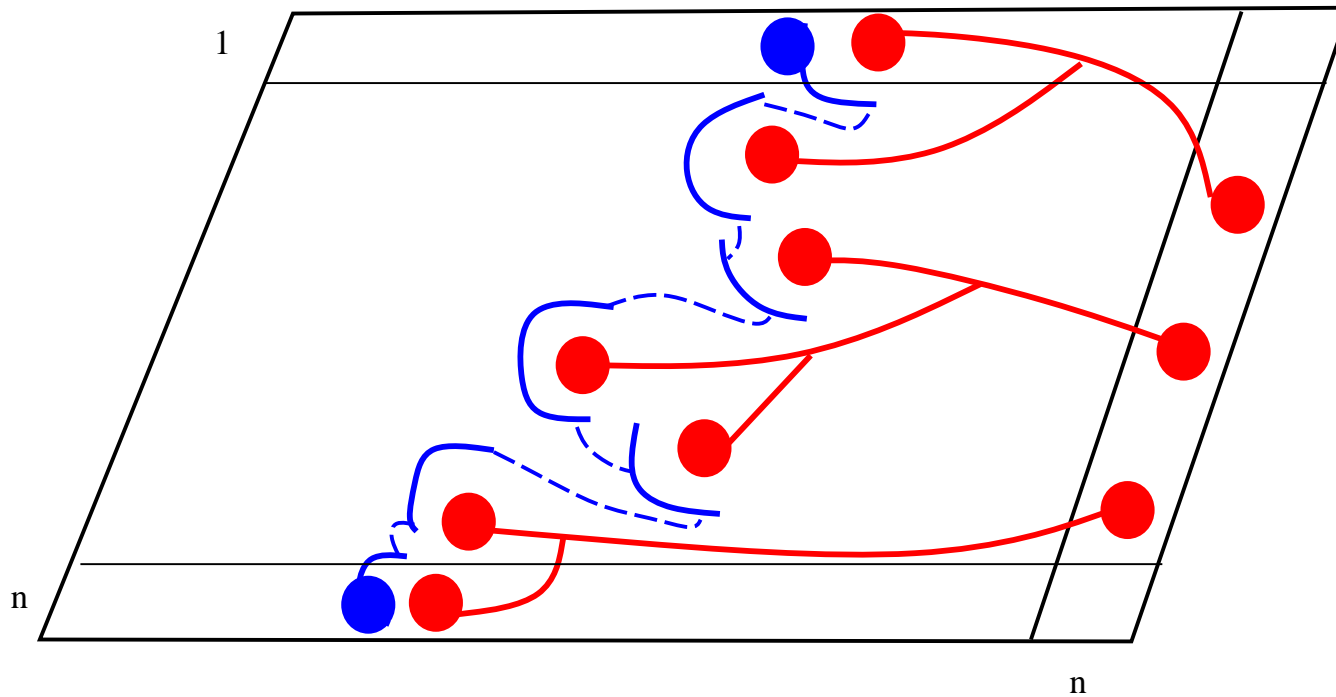
# Illustration of the ideas (1/3)



# Illustration of the ideas (2/3)



# Illustration of the ideas (3/3)



# Strategy-stealing argument

- *The unrestricted form of Hex is a first-player win game. using the “**strategy-stealing**” argument made by John Nash in 1949.*
  - If there is a winning strategy for the second player, the first player can still win by making an arbitrary first move and using the second-player strategy from then on.
    - ▷ *The first player ignores the arbitrary first move by assuming that move does not exist.*
    - ▷ *Hence the second move made by the second player becomes the first move.*
    - ▷ *The third move made by the first player becomes the second move.*
  - If using the second-player strategy requires playing the chosen first move or any move played before, then make another arbitrary move.
    - ▷ *An arbitrary extra move can never be a disadvantage in Hex.*
  - We have obtained a contradiction, and thus the second player cannot win from the initial empty board.
  - Since we have proved there is no draw, and there is always a winner, and both players cannot win at the same time, the first player must have a winning strategy from the initial empty board.

# Strategy-stealing argument: proof (1/3)

- Assume the second player  $P_2$  has a winning function  $f(B)$  that tells the next ply towards winning when seeing the board  $B$ .
  - Assume the initial board position is  $B_0$  which is an empty board.
  - $f(B)$  has a value only for the case  $B$  is a legal position for the second player.
    - ▷  $f(B)$  returns the  $x$ - $y$  coordinates of a location and the color of the piece to play.
  - $rev(m)$ : flip the color and coordinate of a ply  $m$ .
    - ▷ Let  $m = (x_m, y_m)$  be the location to play.
    - ▷ Let  $c$  be the color of the piece to play.
    - ▷ Let  $\bar{c}$  be the color flipped.
    - ▷ Return the location  $(y_m, x_m)$  and the color  $\bar{c}$ .



# Strategy-stealing argument: proof (2/3)

- The steps taken by the first player  $P_1$  to also win:
  - $P_1$  makes an arbitrary first ply  $m_1$ . Call it  $m'$ .
  - $P_2$  uses  $f(B_0 + m_1)$  to make the second ply  $m_2$ .
  - $P_1$  makes the third ply  $m_3 = \text{rev}(f(B_0 + \text{rev}(m_2)))$ .
    - ▷ If  $m_3 = m'$ , then make another arbitrary ply and let it be the new  $m'$ .
  - $P_2$  uses  $f(B_0 + m_1 + m_2 + m_3)$  to make the fourth ply  $m_4$ .
  - $P_1$  makes the fifth ply  $m_5 = \text{rev}(f(B_0 + \text{rev}(m_2) + \text{rev}(m_3) + \text{rev}(m_4)))$ .
    - ▷ If  $m_5 = m'$ , then make another arbitrary ply and let it be the new  $m'$ .
  - $P_2$  uses  $f(B_0 + m_1 + m_2 + m_3 + m_4 + m_5)$  to make the 6th ply  $m_6$ .
  - ...

# Strategy-stealing argument: proof (3/3)

- Hence we know it is not possible for the second player to win.
- We also know these.
  - There is exactly one winner when the board is completely filled.
  - The game is finite.
  - Hence we can enumerate the whole solution search tree.
    - ▷ *In this solution search tree, there is a way for one player to win all of the times no matter the opponent reacts.*
- Since the second player cannot win, the first player must have a winning strategy.

# Strategy-stealing argument: comments

- This is not a constructive proof.
- It only shows the first player has a winning strategy from the initial empty board, not from an arbitrary position.
- The strategy-stealing argument may not be good for other games.
  - An arbitrary extra move can never be a disadvantage in Hex.
  - This may not be true for other games.
- The argument works for any game when
  - there is a way for the first player not to lose at the first ply,
  - it is symmetric,
  - it is **history independent**,
  - it always has exactly one winner, and
    - ▷ *namely, it cannot have a draw by having no winner or two winners,*
  - an arbitrary extra move can always be made and can never be a disadvantage.
    - ▷ *Note: it requires that a player is always possible to place an arbitrary move which may not be true for some games.*

# Properties of Hex

## ■ Variations of Hex

- The **one-move-equalization** rule: one player plays an opening move and the other player then has to decide which color to play for the remainder of the game.
  - ▷ *The revised version is a second-player win game (ultra-weakly).*

## ■ Hex exhibits considerable mathematical structure.

- Hex in its general form has been proved to be PSPACE-complete by Even and Tarjan in 1976 by converting it to a Shannon switching game.
- The state-space and decision complexities are comparable to those of Go on an **equally-sized** board.

## ■ Solutions

- (Weakly or strongly) solved on a  $6 * 6$  board in 1994.
- Maybe possible to solve the  $7 * 7$  case.
  - ▷ *The  $7 * 7$  case was solved in 2001. [Yang et. al. 2001]*
- Not likely to solve the  $8 * 8$  version without fundamental breakthroughs.
  - ▷ *The  $8 * 8$  case was solved in 2009. [Henderson et. al. 2009]*

# More divergent games (1/3)

- **Polynmino games: placing 2-D pieces of a connected subset of a square grid to construct a special form.**
  - Pentominoes
  - Domineering
  - Games on smaller boards have been solved.
- **Othello**
  - M. Buro's LOGISTELLO beat the resigning World Champion by 6-0 in 1997.
  - Weakly solved on a  $6 * 6$  board by J. Feinstein in 1993.
    - ▷ *Second player wins*
- **Chess**
  - DEEP BLUE beat the human World Champion in 1997!

# More divergent games (2/3)

## ■ Chinese chess

- Still in progress.
- Professional 7-dan since 2007.

## ■ Shogi

- Still in progress.
- Claimed to be professional 2-dan in 2007.
- Defeat a Lady professional player in 2010.
- Defeat a 68-year old 1993 Meijin during 2011 and 2012.

# More divergent games (3/3)

## ■ Go

- 5 by 5 Go was solved in 2002.
  - ▷ *First player wins and takes all cells using 22 plys.*
- Recent success and breakthrough using Monte Carlo UCT based methods between 2004 and 2012.
- Lack major theoretical or practical break through since 2012.
- Amateur 1 – 4 kyu in 2008.
  - ▷ *Beat a professional 8-dan by having an 8-stone advantage.*
  - ▷ *Beaten by a professional 9-dan by giving a 7-stone advantage.*
- Amateur 1 dan in 2010.
- Amateur 3 dan in 2011.
- The program Zen beat a 9-dan professional master at March 17, 2012.
  - ▷ *First game: Five stone handicap and won by 11 points.*
  - ▷ *Second game: four stones handicap and won by 20 points.*
- Solved (19 by 19): AlphaGo beat a human top player by a margin of 4:1 at March 2016, and beat the human top player by 3:0 at May 2017.

# Table of complexity

Game	$\log_{10}(\text{state-space})$	$\log_{10}(\text{game-tree size})$
Nine Men's Morris	10	50
Pentominoes	12	18
Awari	12	32
Kalak(6,4)	13	18
Connect-four	14	21
Domineering (8 * 8)	15	27
Dakon-6	15	33
Checkers	21	31
Othello	28	58
Qubic	30	34
Draughts	30	54
Chess	46	123
Chinese chess	48	150
Hex (11 * 11)	57	98
Shogi	71	226
Renju (15 * 15)	105	70
Go-Moku (15 * 15)	105	70
Go (19 * 19)	172	360



# State-space versus game-tree size

- In 1994, the boundary of solvability by complete enumeration was set at  $10^{11}$ .
  - The current estimation is about  $10^{13}$  (since the year 2007).
- It is often possible to use heuristics in searching a game tree to cut the number of nodes visited tremendously when the structure of the game is well studied.
  - Example: Connect-Four.
  - Good heuristics for some games are easier to design than the others.

# Methods developed for solving games

## ■ Brute-force methods

- Retrograde analysis
- Enhanced transposition-table methods

## ■ Knowledge-based methods

- Threat-space search and  $\lambda$ -search
- Proof-number search
- Depth-first proof-number search
- Pattern search

- ▷ To search for *threat patterns*, which are collections of cells in a position.
- ▷ A threat pattern can be thought of as representing the *relevant area* on the board, an area that human players commonly identify when analyzing a position.

## ■ Recent advancements:

- Monte Carlo UCT based game tree simulation.
  - ▷ Monte Carlo method has a root from statistic.
  - ▷ Biased sampling.
  - ▷ Using methods from machine learning.
  - ▷ Combining domain knowledge with statistics.
- Combining searching with Deep learning.

# Brute-force versus knowledge-based methods

- Games with both a relative low state-space complexity and a low game-tree complexity have been solved by both methods.
  - **Category 1**
  - Connect-four and Qubic
- Games with a relative low state-space complexity have mainly been solved with brute-force methods.
  - **Category 2**
  - Namely by constructing endgame databases
  - Nine Men's Morris
- Games with a relative low game-tree-complexities have mainly been solved with knowledge-based methods.
  - **Category 3**
  - Namely, by intelligent (heuristic) searching
  - Sometimes, with the helps of endgame databases
  - Go-Moku, Renju, and  $k$ -in-a-row games

# Advantage of the initiative

- **Theorem (or argument) made by Singmaster in 1981: The first player has advantages.**
  - **Two kinds of positions**
    - ▷ *P-positions: the previous player can force a win.*
    - ▷ *N-positions: the next player can force a win.*
  - **Arguments**
    - ▷ *For the first player to have a forced win, just one of the moves must lead to a P-position.*
    - ▷ *For the second player to have a forced win, all of the moves must lead to N-positions.*
    - ▷ *It is easier to the first player to have a forced win assuming all positions are randomly distributed.*
    - ▷ *Can be easily extended to games with draws.*
- **Remarks:**
  - **One small boards, the second player is able to draw or even to win for certain games.**
  - **Cannot be applied to the infinite board.**

# How to make use of the initiative

- **A potential universal strategy for winning a game:**
  - Try to obtain a small advantage by using the initiative.
    - ▷ *The opponent must react adequately on the moves played by the other player.*
  - To reinforce the initiative the player searches for threats, and even a sequence of threats using an evaluation function  $E$ .
  - Force the opponent to always play the moves you expected.
- **Threat-space search**
  - Search for threats only!

# Offsetting the initiative

- An example of a game with a huge initiative:
  - A connection  $mn1$ -game.
    - ▷ 一子棋 was mentioned in 張系國著名小說”棋王”(1978年出版).
  - A connection  $mn2$ -game.
  - A connection  $mn3$ -game.
  - For a connection  $mn_i$ -game, you can have a feeling that the advantage given to the first player through initiative is gradually lessened when  $i$  gets larger.
- Need to offset the initiative.
  - The offsetting rule must be simple.
  - The revised game must be as **fair** as possible.
    - ▷ *It is difficult to prove a game is fair.*
    - ▷ *Example: Paper-scissor-stone is fair.*
  - The revised game needs be fun to play with.
  - The revised game cannot be too much different from the original game.
- Knowing how to properly offsetting the initiative may uncover some fundamental properties of the game such as its level of difficulty.

# Examples (1/2)

- Enforce rules so that the first player cannot win by selective patterns.
  - Renju.
    - ▷ *Still first-player win.*
  - Go (19 \* 19).
    - ▷ *The first player must win by more than 7 stones.*
    - ▷ *Komi = 7.5 in 2011.*
    - ▷ *The value of Komi changes with the time and maybe different because of using different set of rules.*
- The **one-move-equalization** rule: one player plays an opening move and the other player then has to decide which color to play for the remainder of the game.
  - ▷ *Hex.*
  - ▷ *Second-player win.*

# Examples (2/2)

- **The first move plays one stone, the rest plays two stones each.**
  - ▷ *Connect 6.*
  - ▷ *Intuitively, in each turn the initiative goes to different players alternatively.*
  - ▷ *Still not able to prove the game is fair (in 2016).*
- **The first player uses less resource.**
  - For example: using less time.
    - ▷ *Chinese chess.*
  - A resource-auctioning scheme.
- **General rules to redesign a game to make it fair are unknown and a very good and challenging research topic.**



# Conclusions

- **The knowledge-based methods mostly inform us on the structure of the game, while exhaustive enumeration rarely does.**
- **Many ad-hoc recipes are produced currently.**
  - The database can be used as a corrector or verifier of strategies formulated by human experts.
- **It may be hopeful to use data mining techniques to obtain cross-game methods.**
  - Currently not very successful.

# Comments

- Can combine knowledge-based method with exhaustive enumeration.
  - For converging games, build endgame databases when the remaining state spaces is manageable.
    - ▷ *Example: build endgames with at most 5 pieces in Chess and stop searching when the number of pieces on the board is less than 6.*
  - For diverging games, pre-compute all possible opening moves and solve them one by one in sequence or in parallel.
- This is different from the usage of pattern databases in solving one-player games.
  - Patterns are used to guide the search in solving one-player games.
  - Endgame databases are used here to stop the search earlier. The idea has a flavor like that of bi-directional search.

# 1990's Predictions — 2000's Status

- Predictions were made in 1990 [Allis et al 1991] for the year 2000 concerning the expected playing strength of computer programs.

solved	over champion	world champion	grand master	amateur
<b>Connect-four</b>	Checkers (8 * 8)	Chess	<b>Go (9 * 9)</b>	<b>Go (19 * 19)</b>
<b>Qubic</b>	<b>Renju</b>	Draughts (10 * 10)	Chinese chess	
<b>Nine Men's Morris</b>	<b>Othello</b>		Bridge	
<b>Go-Moku</b>	Scrabble			
Awari	Backgammon			

- color code

- **Green:** Performs much better than expected
- **Red:** right on the target.
- **Black:** have some progress towards the target.
- **Blue:** not so.

# Predictions for 2010

- Predictions were made at the year 2000 for the year 2010 concerning the expected playing strength of computer programs.

<b>solved</b>	<b>over champion</b>	<b>world champion</b>	<b>grand master</b>	<b>amateur</b>
<b>Awari</b>	<b>Chess</b>	<b>Go (9 * 9)</b>	<b>Bridge</b>	<b>Go (19 * 19)</b>
<b>Othello</b>	<b>Draughts (10 * 10)</b>	<b>Chinese chess</b>	<b>Shogi</b>	
<b>Checkers (8 * 8)</b>	<b>Scrabble</b>	<b>Hex</b>		
	<b>Backgammon</b>	<b>Amazons</b>		
	<b>Lines of Action</b>			

# Predictions for 2010 – Status

- My personal opinion about the status of Prediction-2010 at October, 2010, right after the Computer Olympiad held in Kanazawa, Japan.

solved	over champion	world champion	grand master	amateur
<b>Awari</b>	<b>Chess</b>	<b>Go (9 * 9)</b>	<b>Bridge</b>	<b>Go (19 * 19)</b>
<b>Othello</b>	<b>Draughts (10 * 10)</b>	<b>Chinese chess</b>	<b>Shogi</b>	
<b>Checkers (8 * 8)</b>	<b>Scrabble</b>	<b>Hex</b>		
	<b>Backgammon</b>	<b>Amazons</b>		
	<b>Lines of Action</b>			

- color code
  - **Red**: right on the target.
  - **Black**: have some progress towards the target.
  - **Blue**: not so.

# References and further readings (1/2)

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